# Electrocyclic Reactions of 1-Substituted 1,3,5,7-Octatetraenes. An ab Initio Molecular Orbital Study of Torquoselectivity in Eight-Electron Electrocyclizations 

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#### Abstract

The effects of substituents on the conrotatory electrocyclizations of 1 -substituted cis,cis-1,3,5,7-octatetraenes have been studied with ab initio molecular orbital theory. The results are compared to the conrotatory electrocyclic ring openings of 3 -substituted cyclobutenes. Geometry optimizations employed restricted Hartree-Fock calculations and the 3-21G basis set. Electron correlation energies were calculated using second-order Moller-Plesset theory and the $6-31 \mathrm{G}^{*}$ basis set. The transition structure for the conrotatary electrocyclization of cis,cis-1,3,5,7-octatetraene has a helical structure. The steric effects of the substituents direct the stereoselectivities of conrotatory electrocyclizations of 1 -substituted cis,cis-1,3,5,7-octatetraenes. This contrasts to the conrotatory ring openings of 3 -substituted cyclobutenes, where the electronic nature of the substituent directs the stereoselectivities of the conrotatory ring openings.


## Introduction

The electrocyclic reactions of polyenes involve the rotation of the terminal double bonds. For butadiene-cyclobutene interconversions, we have shown how the electronic nature of the substituent influences the direction of rotation of the termini. ${ }^{1}$ Here we extend the study of substituent effects to the electrocyclizations of 1 -substituted cis,cis-1,3,5,7-octatetraenes.

The interconversion of cis,cis-1,3,5,7-octatetraene and cis,cis,cis-$1,3,5$-cyclooctatriene is an example of an eight-electron conrotatory electrocyclic process according to the Woodward-Hoffmann rules. ${ }^{2}$ In a previous study of this process, we showed that the

transition structure has a helical geometry. ${ }^{3}$ This electrocyclization is fast at room temperature ${ }^{4}$ with a measured activation energy of $17.0 \mathrm{kcal} / \mathrm{mol} .^{5}$ Abinitio molecular orbital calculations overestimate the activation energy at the RHF level ( $32.8 \mathrm{kcal} /$ mol by RHF/6-31G* optimization) and underestimate the activation energy at the MP2 level, giving a value of $8.4 \mathrm{kcal} / \mathrm{mol}$ at the MP2/6-31G*//RHF/6-31G ${ }^{*}+$ ZPE level of theory. ${ }^{3}$

The electrocyclic interconversions of several 1 -substituted 1,3,5,7-octatetraenes and 7-substituted 1,3,5-cyclooctatrienes have been studied experimentally. ${ }^{6}$ Generally, the equilibrium lies toward the cyclooctatriene, although conjugating substituents move the equilibrium toward the octatetraene. The rates and stereochemistries of most of these electrocyclic reactions are not known. Marvell and Seubert reported indirect evidence that tcct-

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Figure 1. RHF/6-31G* conrotatory transition structure for the electrocylic interconversion of 1,3,5-cyclooctatriene and cis,cis-1,3,5,7octatetraene. The transition vector is shown. Bond lengths are in angstroms and bond angles are in degrees.
and ccct-2,4,6,8-decatetraene cyclize form trans- and cis-7,8-dimethylbicyclo[4.2.0]octa-2,4-diene, respectively. ${ }^{7}$ Subsequently, Huisgen and co-workers published a series of papers on the rates of electrocyclizations of tcct-, tccc-, and cccc-2,4,6,8-

[^1]Table I. Total Energies of Reactants, Transition Structures, and Products for the Electrocyclizations of 1-Substituted 1,3,5,7-Octatetraenes ${ }^{a}$

| structure | AM1 | RHF/3-21G | ZPE | IMF | RHF/6-31G* ${ }^{\text {b }}$ | MP2/6-31G* ${ }^{\text {a }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1,3,5,7-octatetraene | 0.09246 | -306.972 17 | 103.8 |  | -308.690 33 | -309.69295 |
| cis-1-fluoro-1,3,5,7-octatetraene | 0.01211 | -405.294 11 | 99.2 |  | -407.53880 | -408.710 88 |
| trans-1-fluoro-1,3,5,7-octatetraene | 0.01147 | -405.29106 | 98.9 |  | -407.53793 | -408.709 72 |
| cis-1-methyl-1,3,5,7-octatetraene | 0.07814 | -345.79236 | 122.8 |  | -347.72681 | -348.861 49 |
| trans-1-methyl-1,3,5,7-octatetraene | 0.07619 | -345.795 30 | 122.6 |  | -347.729 94 | -348.864 27 |
| cis-1-formyl-1,3,5,7-octatetraene | 0.04129 | -419.06279 | 111.1 |  | -421.416 50 | -422.717 34 |
| trans-1-formyl-1,3,5,7-octatetraene | 0.03924 | -419.064 75 | 110.9 |  | -421.42194 | -422.72177 |
| 1,3,5-cyclooctatriene | 0.05952 | -306.988 38 | 106.2 |  | -308.706 39 | -309.718 56 |
| 1-fluoro-1,3,5-cyclooctatriene | $-0.00948$ | -405.31084 | 101.4 |  | -407.55921 | -408.738 88 |
| 1-methyl-1,3,5-cyclooctatriene | 0.05273 | -345.809 24 | 125.1 |  | -347.740 82 | -348.88719 |
| 1-formyl-1,3,5-cyclooctatriene | 0.01534 | -419.073 40 | 112.5 |  | -421.426 33 | -422.73780 |
| TS (parent) | 0.12238 | -306.928 99 | 104.5 | $755.9 i$ | -308.63796 | -309.679 39 |
| TS (fluoro in) | 0.05500 | -405.24473 | 99.5 | $815.2 i$ | -407.48110 | -408.696 23 |
| TS (fluoro out) | 0.04286 | -405.248 23 | 99.3 | $815.6 i$ | -407.485 29 | -408.696 84 |
| TS (methyl in) | 0.11827 | -345.74319 | 123.5 | $751.0 i$ | -347.66740 | -348.846 97 |
| TS (methyl out) | 0.10975 | -345.75041 | 123.3 | $768.4 i$ | -347.67508 | -348.851 28 |
| TS (formyl in) | 0.07860 | -419.01173 | 111.1 | 759.9i | -421.359 84 | -422.703 31 |
| TS (formyl out) | 0.07166 | -419.02100 | 111.3 | $751.4 i$ | -421.36713 | -422.708 57 |

${ }^{a}$ Energies are in hartrees, zero-point energies in kcal/mol, and imaginary vibrational frequencies in $\mathrm{cm}^{-1} .{ }^{b}$ Single-point energy evaluation on the optimized RHF/3-21G geometries.

Table II. Relative Energies ( $\mathrm{kcal} / \mathrm{mol}$ ) of the Reactants, Transition Structures, and Products for the Electrocyclizations of 1-Substituted 1,3,5,7-Octatetraenes

| structure | AM1 | RHF/3-21G | RHF/6-31G*a | MP2/6-31G*a | MP2/6-31G*a + ZPE |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1,3,5,7-octatetraene | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| TS | 18.8 | 27.1 | 32.9 | 8.5 | 9.2 |
| 1,3,5-cyclooctatriene | -20.7 | -10.2 | -10.1 | -16.1 | -13.7 |
| cis-1-fluoro-1,3,5,7-octatetraene | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| TS (fluoro in) | 26.9 | 31.0 | 36.2 | 9.2 | 9.5 |
| 7-fluoro-1,3,5-cyclooctatriene | -13.5 | -10.5 | -12.8 | -17.6 | -15.4 |
| trans-1-fluoro-1,3,5,7-octatetraene | 0.0 |  |  |  |  |
| TS (fluoro out) | 19.7 | 26.9 | 33.0 | 8.1 | 8.5 |
| 7-fluoro-1,3,5-cyclooctatriene | -13.1 | -12.4 | -13.4 | -18.3 | -15.8 |
| cis-1-methyl-1,3,5,7-octatetraene | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| TS (methyl in) | 25.2 | 30.9 | 37.3 | 9.1 | 9.8 |
| 7-methyl-1,3,5-cyclooctatriene | -15.9 | -10.6 | -8.8 | -16.1 | -13.8 |
| trans-1-methyl-1,3,5,7-octatetraene | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| TS (methyl out) | 21.1 | 28.2 | 34.4 | 8.2 | 8.9 |
| 7-methyl-1,3,5-cyclooctatriene | -14.7 | -8.8 | -6.8 | -14.4 | -11.9 |
| cis-1-formyl-1,3,5,7-octatetraene | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| TS (formyl in) | 23.4 | 32.0 | 35.6 | 8.8 | 8.8 |
| 7-formyl-1,3,5-cyclooctatriene | -16.3 | -6.7 | -6.2 | -12.8 | -11.4 |
| trans-1-formyl-1,3,5,7-octatetraene | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| TS (formyl out) | 22.9 | 27.5 | 34.4 | 8.3 | 8.7 |
| 7 -formyl-1,3,5-cyclooctatriene | -15.0 | -5.4 | -2.8 | -10.1 | -8.5 |

${ }^{a}$ Single-point energy evaluation on the optimized RHF/3-21G geometries.
decatetraene. ${ }^{8}$ The tect isomer cyclizes fastest, the tecc isomer next, and the cccc isomer the slowest. ${ }^{8}$ In cases where the stereochemistry of an electrocyclic ring opening of a 7 -substituted cyclooctatriene is known, the substituent predominately rotates outward. ${ }^{9-11}$

The stereoselectivities of electrocyclic reactions have been shown to be strongly influenced by the electronic properties of substituents. The ring openings of 3 -substituted cyclobutenes provide many examples of this in both experimental ${ }^{12,13}$ and theoretical ${ }^{1}$ work. The electronic properties of substituents have also been shown to affect the stereoselectivities of the electrocyclizations of 1 -substituted pentadienyl cations ${ }^{14}$ and the
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electrocyclic ring openings of 2-substituted oxiranes and aziridines. ${ }^{15}$ In the six-electron disrotatory electrocyclizations of 1 -substituted $1,3,5$-hexatrienes, steric factors become more important and electronic effects are less important. ${ }^{16}$

## Computational Procedure

Ab initio molecular orbital calculations were performed with restricted Hartree-Fock theory using the GAUSSIAN 88 and 90 programs. ${ }^{17}$ The $3-21 \mathrm{G}^{18}$ basis set was employed for the RHF geometry optimizations.
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Figure 2. RHF/6-31G* transition structure for the electrocylic interconversion of cyclobutene and butadiene. The transition vector is shown.

Harmonic vibrational frequencies were calculated to confirm the nature of all stationary points. Single-point energy evaluations were performed on the RHF/3-21G-optimized geometries using the $6-31 \mathrm{G}^{* 19}$ basis set and second-order Moller-Plesset perturbation theory. ${ }^{20}$ Preliminary calculations were carried out using the semiempirical AM1 method. ${ }^{21}$

There is concern that transition states may be poorly described by RHF wave functions. This is certainly true for reactions which form a biradical. However, we have investigated pericyclic reactions very extensively, including a comparison of RHF and MCSCF results. ${ }^{3}$ For electrocyclizations, both produce very similar results. In our previous studies on the closely related cyclobutene ring opening, we have not found a significant change in the geometry of the calculated transition structures with change in the basis set or methodology. ${ }^{22}$ Goddard et al. have studied the cyclobutene ring opening using CASSCF-level calculations. ${ }^{23}$ The CASSCF transition structure is not very different from the MP2/6$31 \mathrm{G}^{*}$, RHF/6-31G*, and RHF/3-21G transition structures. The most significant difference is a lengthening of the breaking bond by $0.1 \AA$. A general discussion may be found in ref 3 b .

## Results and Discussion

The computed transition structure for the conrotatory electrocyclization of cis,cis-1,3,5,7-octatetraene is shown in Figure 1. The predicted activation energy is $8.4 \mathrm{kcal} / \mathrm{mol}$, and the predicted energy of reaction is $-14.2 \mathrm{kcal} / \mathrm{mol}$ at the MP2 $/ 6$ $31 \mathrm{G}^{*} / / \mathrm{RHF} / 6-31 \mathrm{G}^{*}+$ ZPE level of theory. ${ }^{3}$ The forming bond length is $2.20 \AA$, which is typical of pericyclic reactions. ${ }^{3}$ This conrotatory process is quite different from that of the electrocyclic ring opening of cyclobutene. The transition vector of the 1,3,5,7-

[^2]Table III. Activation Energies and Relative Energies of the Transition Structures for Inward and Outward Rotation of the Substituent for the Ring Opening of 7-Substituted 1,3,5-Cyclooctatrienes ${ }^{a}$

| substituent | basis set | $E_{\text {a }}(\mathrm{in})$ | $E_{\text {a }}$ (out) | $\Delta E_{\mathrm{a}}{ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: |
| F | AM1 | 40.5 | 32.8 | 7.7 |
|  | 3-21G | 41.5 | 39.3 | 2.2 |
|  | 6-31G* ${ }^{\text {c }}$ | 49.0 | 46.4 | 2.6 |
|  | MP2/6-31G* ${ }^{\text {c }}$ | 26.8 | 26.3 | 0.4 |
|  | MP2/6-31G* + ZPE | 24.9 | 24.1 | 0.8 |
| $\mathrm{CH}_{3}$ | AM1 | 41.1 | 35.8 | 5.3 |
|  | 3-21G | 41.4 | 36.9 | 4.5 |
|  | 6-31G* ${ }^{\text {c }}$ | 46.1 | 41.3 | 4.8 |
|  | MP2/6-31G* ${ }^{\text {c }}$ | 25.2 | 22.5 | 2.7 |
|  | MP2/6-31G* + ZPE | 23.6 | 20.7 | 2.9 |
| CHO | AM1 | 39.7 | 35.3 | 4.4 |
|  | 3-21G | 38.7 | 32.9 | 5.8 |
|  | 6-31G* ${ }^{\text {c }}$ | 41.7 | 37.1 | 4.6 |
|  | MP2/6-31G* ${ }^{\text {c }}$ | 21.6 | 18.3 | 3.3 |
|  | MP2/6-31G ${ }^{*}$ c + ZPE | 20.2 | 17.1 | 3.1 |

${ }^{a}$ Energies are in kcal/mol. ${ }^{b} \Delta E_{\mathrm{a}}=E_{\text {in }}-E_{\text {out }} .{ }^{c}$ Single-point energy evaluation on the optimized RHF/3-21G geometries.





Figure 3. RHF/3-21G transition structures for the conrotatory electrocyclization of cis- and trans-1-fluoro-1,3,5,7-octatetraene. Two views of each transition structure are shown.
octatetraene ring closure is almost entirely composed of the motion of the two carbon termini toward each other as well as motions of the vinyl hydrogens at the $1,2,5$, and 6 positions (Figure 1). ${ }^{3}$ It is a conrotatory process that involves rotation about the CC bonds twice removed from the forming CC bond. By contrast, the transition vector for the conrotatory ring opening of cyclobutene primarily involves motion of the hydrogens attached to the carbon atoms of the breaking CC bond to produce a pronounced rotation of the developing $\mathrm{CH}_{2}$ termini of the forming diene (Figure 2).

In the cyclobutene ring opening, the electronic contribution of the substituent is maximized while the steric effects are minimized. Upon inward rotation, the substituent orbitals overlap with the remote terminus of the breaking bond. When a substituent orbital is doubly occupied, this leads to a repulsive cyclic four-electron interaction. Consequently, outward rotation is favored. If the substituent orbital is vacant, then inward rotation is favored to maximize the cyclic two-electron stabilization. ${ }^{1}$

In the octatetraene cyclization, the inward and outward substituents have about the same relationship with the remote terminus of the forming bond. Consequently, a smaller electronic effect upon stereoselectivity is expected. The total and relative energies of the reactants, transition structures, and products for





Figure 4. RHF/3-21G transition structures for the conrotatory electrocyclizations of cis- and trans-1-methyl-1,3,5,7-octatetraene. Twoviews of each transition structure are shown.
the electrocyclic ring closure of three 1 -substituted $1,3,5,7$ octatetraenes have been calculated and are shown in Tables I and II. The activation energies for electrocyclizations of the cis-1-fluoro- and cis-1-methyl-1,3,5,7-octatetraenes are 0.3 and 0.6 $\mathrm{kcal} / \mathrm{mol}$ larger than the activation energy for the electrocyclization of $1,3,5,7$-octatetraene, while the activation energy for the electrocyclization of cis-1-formyl-1,3,5,7-octatetraene is 0.4 $\mathrm{kcal} / \mathrm{mol}$ smaller (without ZPE corrections it is $0.3 \mathrm{kcal} / \mathrm{mol}$ larger). The steric crowding of the inside position is somewhat larger in the transition structure than in the tetraene. The trans isomers have $0.2-0.4 \mathrm{kcal} / \mathrm{mol}$ lower activation energies for cyclization than the parent compound. Each of these substituents stabilizes the transition structures slightly. The energies of reaction are influenced by the substituent interactions with the polyene. Thus, fluorine destabilizes the tetraene relative to the triene because it prefers a saturated position. Methyl has a small effect, while formyl stabilizes the tetraene to a significant extent through extended conjugation with the $\pi$-system.

The equilibrium between 1,3,5,7-octatetraenes, and 1,3,5cyclooctatrienes generally favors the cyclooctatrienes. To assess torquoselectivity without corrections for ground-state substituent effects, it is easier to compare the ring openings of 7 -substituted





Figure 5. RHF/3-21G transition structures for the conrotatory electrocyclization of cis- and trans-1-formyl-1,3,5,7-octatetraene. Two views of each transition structure are shown.

1,3,5-cyclooctatrienes with those of 3 -substituted cyclobutenes. The activation energies for inward and outward rotation of several 7 -substituted cyclooctatrienes are given in Table III. The substituents range from a moderately strong $\pi$-electron donor (F) to a weak donor $\left(\mathrm{CH}_{3}\right)$ to a strong electron acceptor (CHO). The transition structures for these reactions are shown in Figures 3-5. The geometries of these transition structures are remarkably similar to each other and to the parent transition structure. The forming bond lengths range from 2.18 to $2.22 \AA$, while the partial double bond lengths alternate slightly, resembling the octatetraene more than cyclooctatriene values. The activation energies of the corresponding cyclobutene ring openings are given in Table V , while the raw data are given in Table IV. The computed activation energy differences between inward and outward rotations of substituted 3-cyclobutenes have been shown to have a nearly linear dependence on the empirical resonance parameter $\sigma_{\mathrm{R}}{ }^{\circ}{ }^{1} \mathrm{~A}$ graph of the differences of inward and outward activation energies for the three substituted cases of cyclooctatriene and cyclobutene are plotted against $\sigma_{\mathrm{R}}^{\circ}$ in Figure 6. There is a small preference for outward rotation of the substituent in 7 -substituted 1,3,5cyclooctatrienes regardless of its electron-donating or electronaccepting ability. The helical transition structure causes sub-

Table IV. Total Energies of Reactants, Transition Structures, and Products for the Electrocyclic Ring Opening of Cyclobutene and 3-Substituted Cyclobutenes ${ }^{a}$

| structure | AM1 | RHF/3-21G | ZPE | IMF | RHF/6-31G* ${ }^{\text {b }}$ | MP2/6-31G* ${ }^{\text {a }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| cyclobutene | 0.07282 | -154.030 $722^{\text {c.d }}$ | 58.4 |  | -154.898 $31^{\text {d }}$ | -155.407 $75^{\text {c.d }}$ d |
| 3-fluorocyclobutene | -0.001 65 | -252.34960 | 53.5 |  | -253.750 18 | -254.426 33 |
| 3-methylcyclobutene | 0.06322 | -192.85318 | 77.4 |  | -193.935 19 | -194.577 33 |
| 3-formylcyclobutene | 0.02615 | $-266.11751^{e}$ | 65.0 |  | -267.622 $01{ }^{\text {e }}$ | -268.429 14 |
| butadiene | 0.04757 | $-154.05946{ }^{\text {c.d }}$ | 57.8 |  | $-154.91961^{\text {d }}$ | $-155.420711^{\text {c.d }}$ |
| cis-1-fluorobutadiene | -0.033 29 | -252.37802 | 52.9 |  | -253.766 93 | -254.437 14 |
| trans-1-fluorobutadiene | $-0.03262$ | -252.38081 | 53.3 |  | -253.76785 | -254.438 22 |
| cis-1-methylbutadiene | 0.03324 | -192.87980 | 76.9 |  | -193.956 25 | -194.589 15 |
| trans-1-methylbutadiene | 0.03141 | -192.882 39 | 76.7 |  | -193.959 08 | -194.591 66 |
| cis-1-formylbutadiene | -0.003 64 | -266.15000 | 65.1 |  | -267.64560 | -268.44474 |
| trans-1-formylbutadiene | $-0.00553$ | -266.15129 | 64.9 |  | -267.650 94 | -268.448 76 |
| TS (parent) | 0.12913 | $-153.964355^{\text {c.d }}$ d | 56.8 | $899.4 i$ | $-154.82459^{d}$ | $-155.349422^{\text {c.d }}$ |
| TS (fluoro in) | 0.05602 | -252.265 54 | 51.7 | 901.8i | -253.656 25 | -254.35288 |
| TS (fluoro out) | 0.04298 | -252.293 08 | 52.1 | $777.7 i$ | -253.683 31 | -254.377 52 |
| TS (methyl in) | 0.11961 | -192.777 74 | 75.8 | $849.3 i$ | -193.853 55 | -194.51291 |
| TS (methyl out) | 0.11313 | -192.78804 | 75.5 | $813.5 i$ | -193.863 04 | -194.520 87 |
| TS (formyl in) | 0.07455 | -266.062 15 ${ }^{\text {e }}$ | 63.9 | $728.5 i$ | $-267.56152^{e}$ | -268.385 14 |
| TS (formyl out) | 0.07516 | -266.055 $02{ }^{\text {e }}$ | 63.6 | 807.2i | -267.554 $13{ }^{\text {e }}$ | -268.377 18 |

[^3]Table V. Activation Energies and Relative Eneriges of the Transition Structures for Inward and Outward Rotation of the Substituent for the Ring Opening of 3-Substituted Cyclobutenes ${ }^{a}$

| substituent | basis set | $E_{\text {a }}(\mathrm{in})$ | $E_{\text {a }}$ (out) | $\Delta E_{\mathrm{a}}{ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: |
| F | AM1 | 36.2 | 28.0 | 8.2 |
|  | 3-21G | 52.7 | 35.5 | 17.2 |
|  | 6-31G* ${ }^{\text {c }}$ | 58.9 | 42.0 | 16.9 |
|  | MP2/6-31G* ${ }^{\text {c }}$ | 46.1 | 30.6 | 15.5 |
|  | MP2/6-31G* ${ }^{\text {c }}+$ ZPE | 44.3 | 29.2 | 15.1 |
| $\mathrm{CH}_{3}$ | AM1 | 35.4 | 31.3 | 4.1 |
|  | 3-21G | 47.3 | 40.9 | 6.4 |
|  | 6-31G* ${ }^{\text {c }}$ | 51.2 | 45.3 | 5.9 |
|  | MP2/6-31G* | 40.4 | 35.4 | 5.0 |
|  | MP2/6-31G ${ }^{*} c+$ ZPE | 38.8 | 33.5 | 5.3 |
| CHO | AM1 | 30.4 | 30.8 | -0.4 |
|  | 3-21G | 34.7 | 39.2 | $-4.5$ |
|  | 6-31G* ${ }^{\text {c }}$ | 38.0 | 42.6 | -4.6 |
|  | MP2/6-31G* ${ }^{\text {c }}$ | 27.6 | 32.6 | -5.0 |
|  | MP2/6-31G* ${ }^{\text {c }}$ + ZPE | 26.5 | 31.2 | -4.7 |

${ }^{a}$ Energies in kcal/mol. ${ }^{b} \Delta E_{\mathrm{a}}=E_{\text {in }}-E_{\text {out }}{ }^{c}$ SIngle-point energy evaluation on the optimized RHF/3-21G geometries.


Figure 6. Plot of $\Delta E_{a}$ versus $\sigma_{\mathrm{R}}^{\circ}$ for the electrocyclic ring openings of 7 -substituted 1,3,5-cyclooctatrienes and 3 -substituted cyclobutenes.
stituents on the inside or outside to experience essentially the same relationship to the breaking CC bond, since there is no twisting of the breaking bond. Consequently, the electronic nature of the substituent does not play an important role in directing the
rotational preference. Steric effects do cause a small preference for all substituents to rotate outward, ranging from $0.8 \mathrm{kcal} / \mathrm{mol}$ for fluorine to $3.1 \mathrm{kcal} / \mathrm{mol}$ for a formyl group at the MP2/6-31G*//RHF/3-21G + ZPE level. The differences are slightly larger at the RHF levels studied, which may give more reliable numbers for these systems. This will be discussed below.
In the parent reaction (Figure 1), the two outside hydrogens are $2.69 \AA$ from each other while an inside hydrogen is $2.42 \AA$ from the carbon atom adjacent to the other carbon termini. Calculated secondary deuterium isotope effects for the parent electrocyclization yield a smaller $k_{\mathrm{H}} / k_{\mathrm{D}}$ ( 0.93 for inside hydrogen, 0.98 for the outside hydrogen) for the inside hydrogen. ${ }^{3}$ This corresponds to a tighter bending constant for the inside hydrogen, which results from more steric crowding.
The preference for an alkyl group to be outside in the transition structure of cyclization is in agreement with the experimental results of Huisgen et al. ${ }^{8} \Delta H^{*}$ values for cyclization of three decatetraenes have been measured experimentally. They are 15.1 , 17.8 , and $21.8 \mathrm{kcal} / \mathrm{mol}$ for the electrocyclizations of $t c c t-$, $t c c c$-, and cccc-5,7,9-decatetraene. ${ }^{7}$ The tcct isomer, which cyclizes the fastest, has two methyl groups rotating out. The tecc isomer cyclizes second fastest and has one methyl group rotating out and one rotating in. The slowest cyclizing isomer, cccc, has two methyl groups rotating in. The change from a methyl out to a methyl in increases the activation energy by 2.7 and $4.0 \mathrm{kcal} / \mathrm{mol}$ (tcct $\rightarrow$ ccct, and ccct $\rightarrow$ cccc, respectively). Rotation of a second methyl group inward produces an additional Me-Me steric interaction. A change of only $0.9 \mathrm{kcal} / \mathrm{mol}$ is predicted at the MP2/6-31G* level. However, RHF calculations provide much better predictions. With the $3-21 \mathrm{G}$ basis set, a $2.7-\mathrm{kcal} / \mathrm{mol}$ difference is predicted, while with the 6-31G* basis set, a 2.9 $\mathrm{kcal} / \mathrm{mol}$ difference is predicted. Both RHF results are in good accord with the $2.7-\mathrm{kcal} / \mathrm{mol}$ difference observed for the conversion of tect and ccet.

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[^3]:    ${ }^{a}$ Energies are in hartrees, zero-point energies in kcal/mol, and imaginary vibrational frequencies in $\mathrm{cm}^{-1} .{ }^{b}$ Single-point energy evaluation on the optimized RHF/3-21G geometries. ${ }^{c}$ See ref 1a. ${ }^{d}$ See ref $24 .{ }^{e}$ See ref 1 b .

